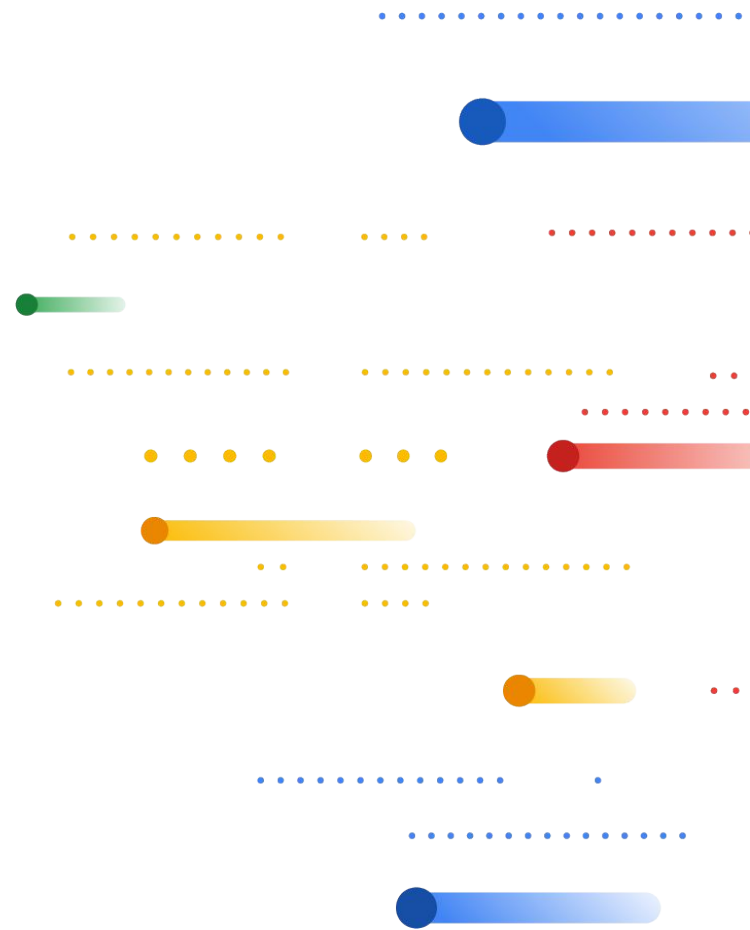


Examining Parameter Uncertainty Through Large Cloud-Based Ensembles

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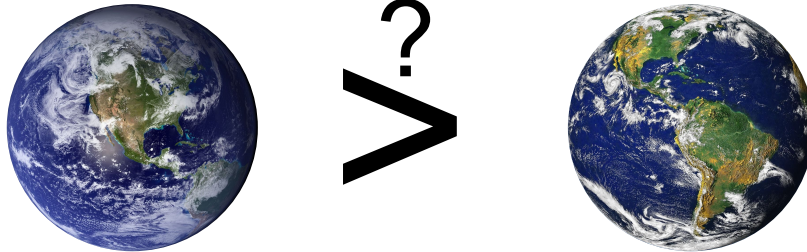
CESM WORKSHOP 2023
Parameter Estimation Cross Working Group
June 12, 2023



CESM and Google Climate & Energy

Aspirational goals: answer questions like

- What global heating mitigation work should Google do?
- How much impact will project A have vs project B?
- (Probably both unknowable — but what *can* we learn?)



Challenges

- Compute environment different than typical clusters for CESM
- Lots of uncertainty in CESM outputs

CESM on Google Cloud

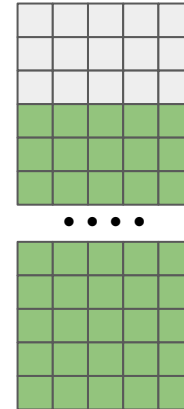
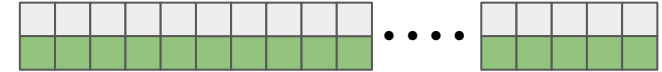
Diffs vs dedicated cluster

- Best price w/ preemptible VMs
 - Fewer network guarantees
 - Failed VMs stall MPI
- ⇒ Focus on single-machine simulations

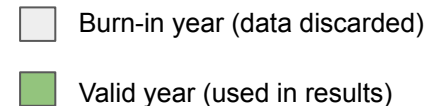
Ensemble shape: wide vs deep

- Why?
 - On one VM, 1° fixed SST: ~50 days for 100-year sim
 -but can easily scale to 1000s of VMs
- Early results: get same stats if we are careful**
- ***Good platform for exploring uncertainties!***

Wide Ensemble (Members x Years)



Deep Ensemble



Contrail Impact

What is the climate impact from contrails?

How big are the error bars on contrail ERF?

Which mitigation strategies are most effective?



Contrail Impact

Sim setup

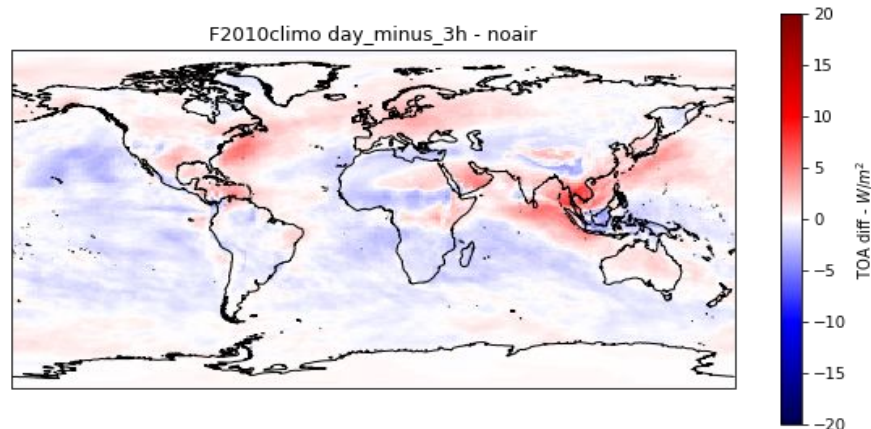
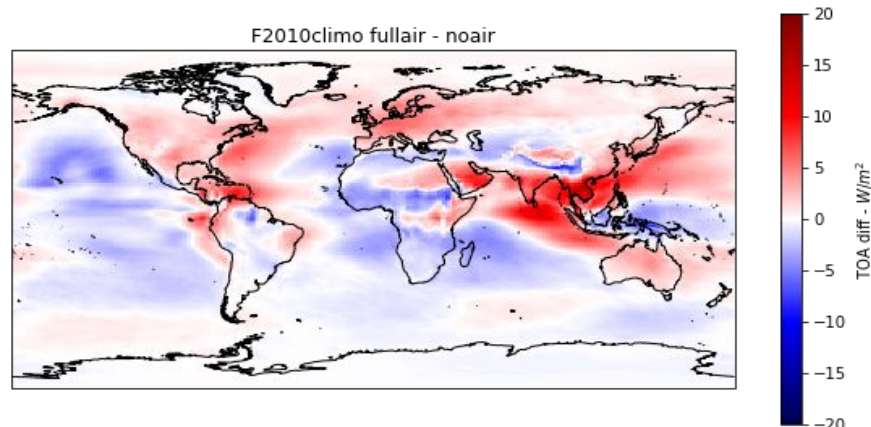
- CAM 6.3; Fixed SST
- Scenarios
 - No aviation
 - Full aviation (FA)
 - Mitigation Strategy (MS)

Measure

- Radiative imbalance at top of atmosphere (TOA)

Explorations last ~4 months

- 83 ensembles
- >10k sim years



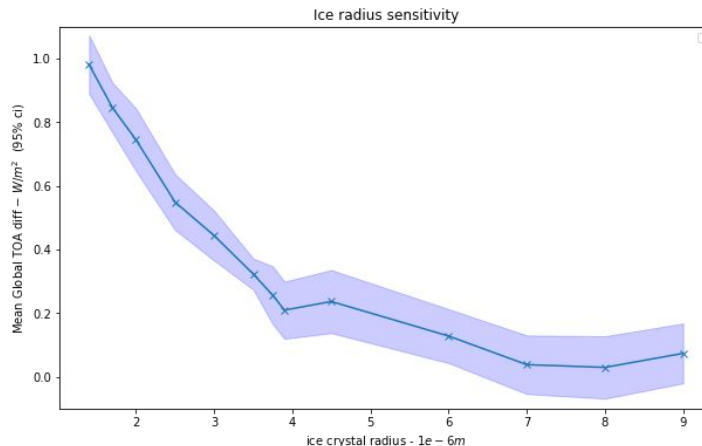
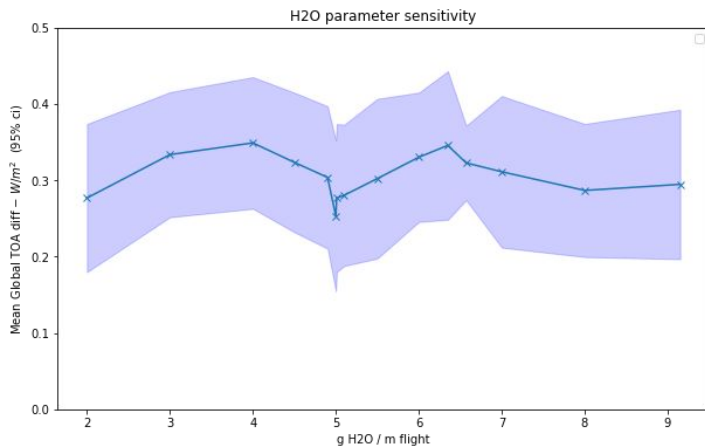
Contrail ERF Error Bars

Variation among ensemble members (aleatoric uncertainty)

- Large SEM vanquished via \sqrt{N}
- Easy to run large ensembles

Are the contrail module parameters correct? (epistemic uncertainty)

- Some choices have a big impact on computed TOA!



NOTE: These graphs are from a set of debugging runs, so the specific TOA values are not relevant.

Contrail Mitigation Effectiveness

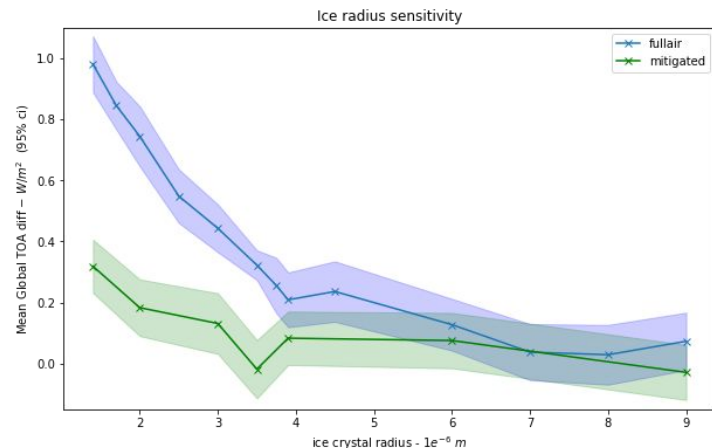
Problem: Baseline warming depends on params

Heavyweight Solution: Many ensembles

- Pick several sets of params
- Run FA and MS ensembles for each
- Compare %mitigated across param vals

More Problems

- Compute costs
- How to compare?



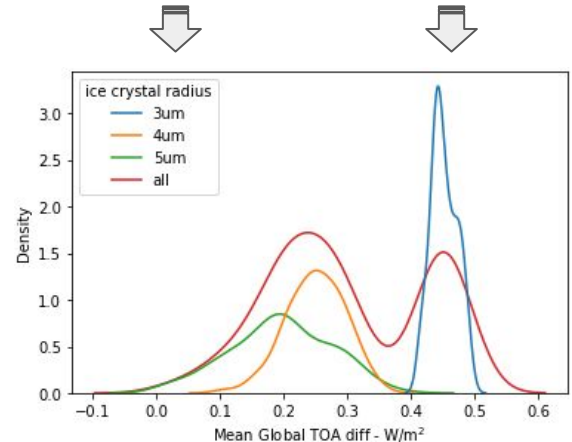
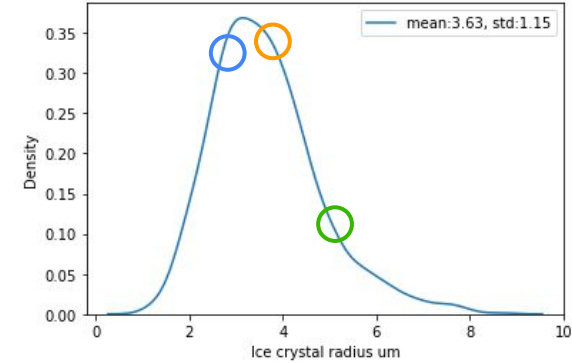
Better Solution: MC Sampling + ANOVA

Intuition

- Pick a reasonable distribution for each param
- Sample params & run sims to get TOA
- Use analysis of variance
 - Extract the experimental effect
 - ...in spite of param diffs

Evaluating mitigation

- Use effect ratio to compare across TOA baselines
- Bootstrap sampling to analyze variance
- 95% CI of ratio $< 1.0 \Rightarrow$ mitigation works!



Regression-based Variance Analysis

Generate Monte-Carlo dataset¹: $\{(TOA_i, FA_i, r_i)\}_{i=1}^n$

- 1) Sample ice radius $r_i \sim f_r$
- 2) Run CESM under baseline ($FA_i=0$) or full air traffic ($FA_i=1, r_i$) scenarios to get TOA_i

Estimate full aviation effect β_1 , with any $g()$ where $E[g(r)] = 0$

$$E[TOA|FA, r] = \beta_0 + FA\{\beta_1 + \beta_2 g(r)\}$$

Note:

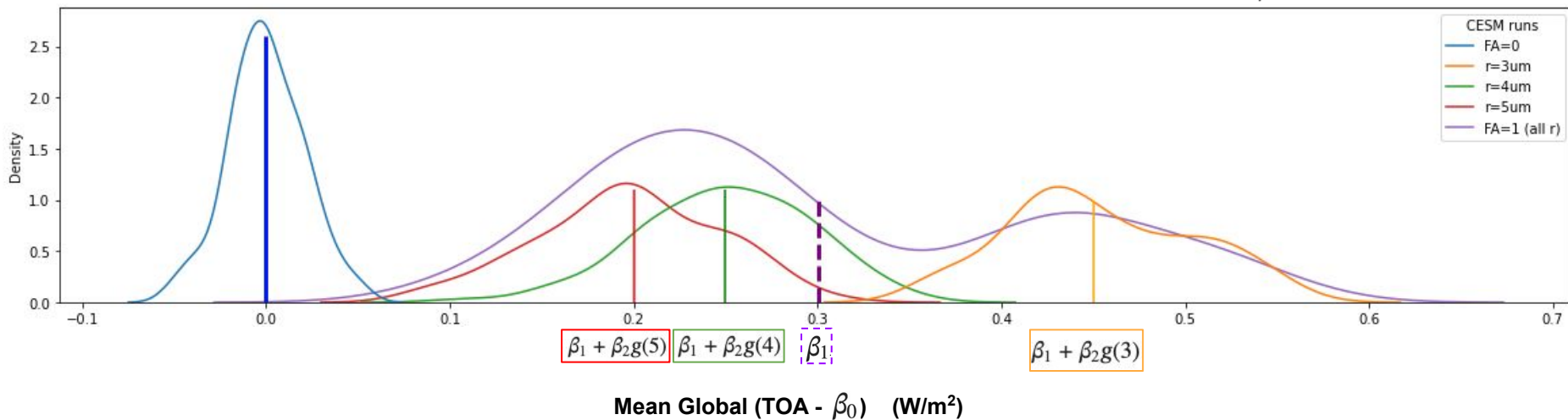
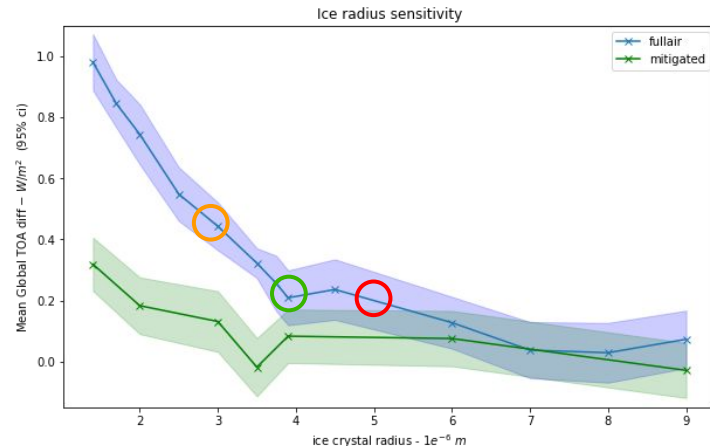
- Baseline TOA is β_0 since $E[TOA|FA = 0] = \beta_0$
- Fullair effect is β_1 since $E_r\{E[TOA|FA = 1, r]\} = \beta_0 + \beta_1$

1. For simplicity, this example uses a single ice radius parameter, but the method applies for vector-valued r

Regression-based Variance Analysis

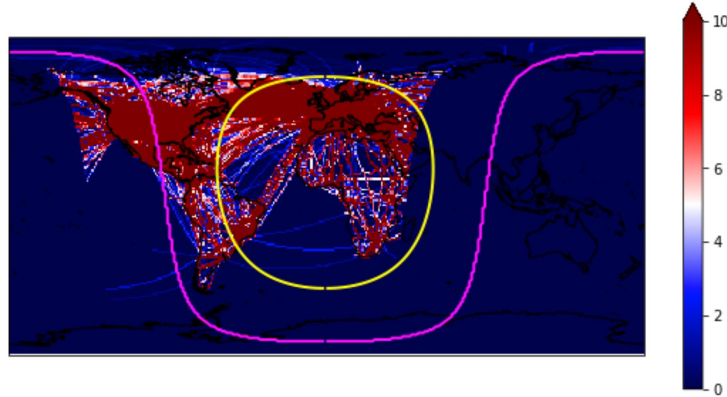
$$E[TOA|FA, r] = \beta_0 + FA\{\beta_1 + \beta_2 g(r)\}$$

Combine simulations with different r_i to estimate β_1 .



Mitigation Strategies

What about turning off air traffic only at night?



Similar MC approach can be used to generate dataset: $\{(TOA_i, MS_i, r_i)\}_{i=1}^m$

Estimate effect of mitigation strategy with:

$$E[TOA|MS, r] = \alpha_0 + MS\{\alpha_1 + \alpha_2 h(r)\}, \quad E[h(r)] = 0$$

Air Traffic Effect Ratio

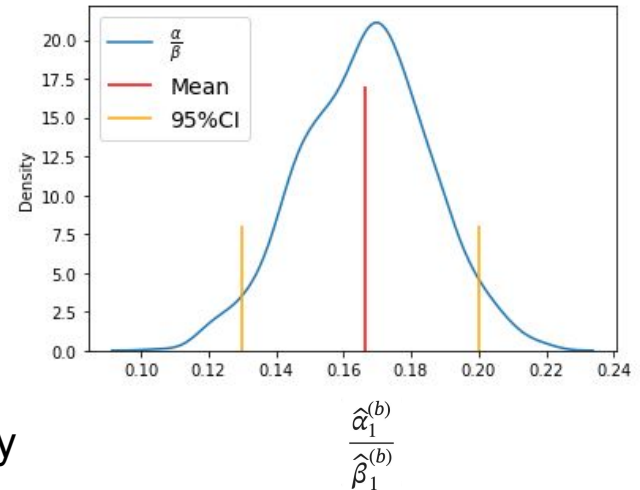
How do different mitigation strategies compare?

$$\begin{array}{l} \text{Mitigation strategy} \\ \text{vs.} \\ \text{full air traffic} \end{array} \quad \frac{E_r\{E[TOA|MS = 1, r] - E[TOA|MS = 0]\}}{E_r\{E[TOA|FA = 1, r] - E[TOA|FA = 0]\}} = \frac{\alpha_1}{\beta_1}$$

How do we account for parameter uncertainties?

Bootstrap for handling epistemic uncertainty:

1. Sample CESM runs from $\left\{ \begin{array}{l} \{(TOA_i, FA_i, r_i)\}_{i=1}^n \\ \{(TOA_j, MS_j, r_j)\}_{j=1}^m \end{array} \right.$
2. Estimate $\hat{\alpha}_1^{(b)}, \hat{\beta}_1^{(b)}, b = 1, \dots, B$
3. Compute ratio $\left\{ \frac{\hat{\alpha}_1^{(b)}}{\hat{\beta}_1^{(b)}} \right\}_{b=1}^B$, and quantiles for uncertainty



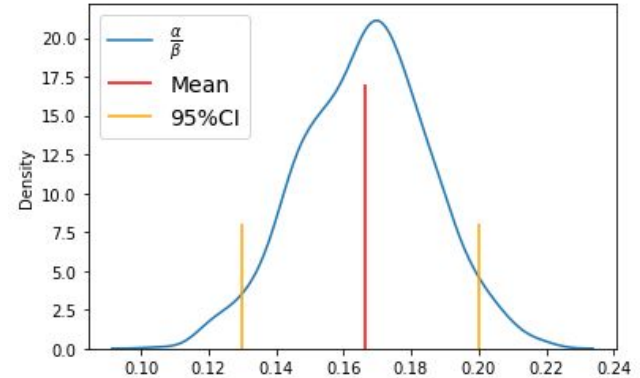
Certainty from Uncertainty?

Compute infrastructure

- Wide parallelization allows rapid exploration
- Short sims good enough (for some cases)

Variance analysis

- Allows conclusions about mitigation effectiveness
 - In spite of aleatoric and epistemic uncertainty
- Reduces compute requirements
 - eg O(500) ensembles instead of O(5000)



$$\frac{\hat{\alpha}_1^{(b)}}{\hat{\beta}_1^{(b)}}$$